Spontaneous Oscillation by Hair Bundles of the Bullfrog’s Sacculus

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One prominent manifestation of mechanical activity in hair cells is spontaneous otoacoustic emission, the unprovoked emanation of sound by an internal ear. Because active hair bundle motility probably constitutes the active process of nonmammalian hair cells, we investigated the ability of hair bundles in the bullfrog’s sacculus to produce oscillations that might underlie spontaneous otoacoustic emissions. When maintained in the normal ionic milieu of the ear, many bundles oscillated spontaneously through distances as great as 80 nm at frequencies of 5–50 Hz. Whole-cell recording disclosed that the positive phase of movement was associated with the opening of transduction channels. Gentamicin, which blocks transduction channels, reversibly arrested oscillation; drugs that affect the cAMP phosphorylation pathway and might influence the activity of myosin altered the rate of oscillation. Increasing the Ca\(^{2+}\) concentration rendered oscillations faster and smaller until they were suppressed; lowering the Ca\(^{2+}\) concentration moderately with chelators had the opposite effect. When a bundle was offset with a stimulus fiber, oscillations were transiently suppressed but gradually resumed. Loading a bundle by partial displacement clamping, which simulated the presence of the accessory structures to which a bundle is ordinarily attached, increased the frequency and diminished the magnitude of oscillation. These observations accord with a model in which oscillations arise from the interplay of the hair bundle’s negative stiffness with the activity of adaptation motors and with Ca\(^{2+}\)-dependent relaxation of gating springs.

Key words: adaptation; amplification; auditory system; mechanoelectrical transduction; negative stiffness; vestibular system

Introduction

The ear is mechanically active. Whether spontaneous or evoked by sound, otoacoustic emissions constitute the most striking evidence that energy-consuming elements within the inner ear can produce work. The ear’s ability to deliver metabolically powered forces results in mechanical amplification: for sound stimuli near threshold, the active process augments vibrations in the mammalian cochlea by >100-fold, thus countering the dissipation caused by viscous drag in the fluid of the inner ear. Amplification of faint stimuli is closely associated with sharp frequency selectivity, because each portion of a receptor organ acts as a highly tuned mechanical resonator that responds preferentially at a natural frequency. Finally, the response of the ear to stimuli of increasing magnitude grows nonlinearly; the basilar membrane of the chinchilla, for example, represents six decades of sound pressure by only two orders of magnitude of vibration (Ruggero et al., 1997). Otoacoustic emissions, amplification, frequency selectivity, and compressive nonlinearity represent four essential characteristics of the active process that enhances detection of mechanical stimuli by the vertebrate inner ear (for review, see Manley, 2000, 2001).

Although amplification in the mammalian cochlea is widely believed to involve membrane-based electromotility by outer hair cells (reviewed in Dallos, 1992; Nobili et al., 1998), the receptor organs of amphibians, reptiles, and birds are not endowed with electromotile cells (He et al., 2003). The ears of nonmammalian tetrapods nevertheless display all four characteristics of the active process (for review, see Manley and Köppl, 1998; Manley, 1999, 2001). The alternative mechanism proposed to underlie the active process in those animals, and perhaps in mammals as well, is active hair bundle motility (for review, see Hudspeth, 1997; Hudspeth et al., 2000; Fettiplace et al., 2001). This process plays the four hallmarks of the active process (Martin and Hudspeth, 2001). A bundle can oscillate spontaneously (Crawford and Fettiplace, 1985; Howard and Hudspeth, 1987a; Denk and Webb, 1992; Benser et al., 1996; Martin and Hudspeth, 1999, 2001; Martin et al., 2000, 2001), a behavior that might underlie spontaneous otoacoustic emissions. The power expended by an oscillating bundle can be funneled into a weak sinusoidal stimulus to amplify the input (Martin and Hudspeth, 1999, 2001). The sensitivity of a bundle is tuned, with the greatest responsiveness at its natural frequency (Martin et al., 2001). Finally, the response of a hair bundle at its natural frequency displays a compressive nonlinearity (Martin and Hudspeth, 2001).

The four characteristics that define the aural active process are signatures of a dynamical system operating near a Hopf bifurcation (Choe et al., 1998; Camalet et al., 2000; Eguíluz et al., 2000; Jülicher et al., 2001; Martin et al., 2001). Such an oscillatory instability may emerge from the interplay of the negative stiffness of a hair bundle (Martin et al., 2000) with the molecular motors responsible for mechanical adaptation (for review, see Hudspeth and Gillespie, 1994; Eatock, 2000; Holt and Corey, 2000). To
strengthen the evidence that this mechanism can mediate active hair bundle movements, we have examined the effects of treatments that affect the mechanical properties of a bundle and the adaptation motor on the ability of a hair cell to oscillate spontaneously.

Materials and Methods

Experimental preparation. Experiments were performed at a room temperature of ~21°C on succulent hair cells from the bulbfrog *Rana catesbeiana*. Each internal ear was dissected in oxygenated standard saline solution containing (in mM): 110 Na$^+$, 2 K$^+$, 4 Ca$^{2+}$, 122 Cl$^-$, 3 D-glucose, and 5 HEPES. After dissection from the labyrinth, the saccular macula was loosened by a 30 min exposure of the apical surface to 40 μg/ml protease type XXIV in N-methyl-D-glucamine (NMDG) endolymph containing (in mM): 2 Na$^+$, 3 K$^+$, 0.25 Ca$^{2+}$, 110 NMDG, 118 Cl$^-$, 3 D-glucose, and 5 HEPES. The otolithic membrane was then lifted from the hair bundles, and the coverslip was secured in a two-compartment experimental chamber (Martin and Hudspeth, 1999).

During most experiments, the standard saline solution in the lower compartment was not exchanged. The upper compartment ordinarily contained oxygenated NMDG endolymph; except when specifically indicated, the results presented here were obtained in the presence of this solution. Some experiments instead used artificial endolymph containing (in mM): 2 Na$^+$, 118 K$^+$, 0.25 Ca$^{2+}$, 118 Cl$^-$, 3 D-glucose, and 5 HEPES. Each solution had a pH of ~7.3 and an osmotic strength of ~230 mmoles/kg.

Enzymes, drugs, and other chemicals were obtained from Sigma (St. Louis, MO).

Kinociliary dissection. After control recordings had been made, kinocilia were detached from individual hair bundles with a horizontally mounted glass microelectrode (Hudspeth and Jacobs, 1979). The tip of the electrode was situated over the hair cell under investigation, then pulled closer in a direction perpendicular to the epithelial surface.

Iontophoresis of Ca$^{2+}$ and drugs. Iontophoresis was used to apply several substances to hair bundles during measurement of their spontaneous oscillation and stiffness. In each instance, a coarse microelectrode, whose resistance would have been on the order of 30 MΩ, was bent to permit an orthogonal approach to the apical surface of a cell, and heat-polished to give resistances of ~5–10 MΩ. The tip of the recording electrode was positioned with a Huxley micromanipulator on the apical surface of a hair cell opposite the kinocilium (Holton and Hudspeth, 1986).

Each recording pipette was tip-filled for ~1 sec with a solution containing (in mM): 110 G$^+$, 3 Mg$^{2+}$, 20 spermine, 114 Cl$^-$, 40 SO$_4^{2-}$, and 5 HEPES. The pipette was then back-filled with an identical solution supplemented with 260 μM amphotericin B that had been dissolved in DMSO, whose concentration in the internal solution was 2% (v/v). When used in the presence of artificial endolymph, this internal solution produced a liquid–junction potential of ~0 mV. A polycationic molecule, spermine, was included in the internal solution because of the difficulty in creating tight seals on the apical membrane of hair cells (Holton and Hudspeth, 1986). The presence of spermine permitted the formation of tight seals within several seconds of applied suction. Like its precursor spermidine, this polycation occurs in cytoplasm at a concentration of ~1 mM as an important counterion to RNA (Igarashi and Kashiwagi, 2000).

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The transduction currents measured in the presence of spermine did not differ in magnitude from those recorded from isolated hair cells (Jaramillo and Hudspeth, 1991; Assad and Corey, 1992; Shepherd and Corey, 1994; Walker and Hudspeth, 1996; Lumpkin and Hudspeth, 1998), for which no special treatment is required to make tight seals. Moreover, control recordings earlier demonstrated no untoward effects of lower concentrations of spermine and spermidine (Holton and Hudspeth, 1986). Because the membrane potential of a hair cell was held either at the resting potential ascertained under current-clamp conditions or at ~70 mV, transduction currents were always inward and it is improbable that a cation such as spermine would have significantly blocked transduction channels.

Microscopic apparatus. Experiments were conducted under an upright microscope (MPS; Zeiss, Jena, Germany) equipped with a 100 W mercury illuminator, an infrared-reflecting hot mirror (K43-842; Edmund Industrial Optics, Barrington, NJ), and a broadband green interference filter (500 ± 40 nm, half-width at half-maximal transmittance; K46-157; Edmund Industrial Optics). The image formed by a 40× water immersion objective lens of numerical aperture 0.75 was further magnified by a 1.6× annular lens. Observations by eye and video microscopy were made with differential interference contrast optics. To increase the signal reaching the photodiodes, the analyzer was relocated from the microscope tube to the eyepiece assembly; moreover, during measurements of hair bundle motion, the polarizer was removed.

Because spontaneous hair bundle movements were sometimes too small or too fast to be detected directly by eye, we also used video microscopy to locate spontaneously active bundles. The image provided by the microscope was relayed through a projection eyepiece of 125 mm focal length or by a 1.5× telescope to a charge-coupled–device camera whose field of view encompassed several hair bundles. Its output was directed to a video image processor (Argus-20; Hamamatsu Photonics, Hamamatsu City, Japan). To highlight hair bundle oscillations, we digitally subtracted from each frame the running average of several consecutive frames.

Mechanical stimulation. Mechanical stimuli were applied by a flexible glass fiber whose tip was attached to the kinociliary bulb of an individual hair bundle. Fibers were fabricated from borosilicate capillaries of 1.2 mm diameter (TW120-3, World Precision Instruments). Each capillary was first reduced with an electrode puller (P-80/PC; Sutter Instruments, Novato, CA) and then pulled finer in a direction perpendicular to its shank with a 120 V solenoid (Howard and Hudspeth, 1988). We found that a fiber of ~500 nm in diameter was best for attachment to the kinociliary bulb. The fiber was trimmed with iridectomy scissors to a length of 100–400 μm. To enhance optical contrast, we coated the fiber with an ~100 nm layer of gold-palladium (Hummer VI; Anatech, Alexandria, VA). The stiffness and drag coefficient of the fiber were, respectively, 80–400 μN m$^{-1}$ and 40–110 nN sec m$^{-1}$, as determined by power spectral analysis of Brownian motion of the tip of the fiber in water. The fiber behaved as a first-order low-pass mechanical filter with a cutoff frequency of 0.2–1.6 kHz.

The fiber was secured by its base to a stack-type piezoelectric actuator (P835.10; Physik Instrumente) driven by a matched power supply (P-870; Physik Instrumente); this actuator provided displacements up to ±1 μm with a bandwidth of 5 kHz. The piezoelectric actuator was in turn mounted on a Huxley micromanipulator, which allowed fine positioning of the tip of the fiber with a submicrometer resolution. The fiber was used both to apply stimuli at the top of a hair bundle and to report bundle movements. Holding the base of the fiber at a fixed position permitted accurate measurement of the spontaneous motion of the bundle.

Displacement monitor. The tip of the fiber was imaged at a magnification of 1000× on a dual photodiode (UV-140-2; EG&G Electro-Optics,
in which $K_{SF}$ represents the stiffness of the stimulus fiber. In combination with Equation 1 for $X_C = 0$, the Fourier transform of Equation 3 yields:

$$\tilde{F}_{SF}(\omega) = -K_{SF}(\omega)\tilde{X}(\omega),$$

in which $K_{EFF}(\omega) = K_{SF}[1 + G(\omega)]$ defines the impedance of the fiber at angular frequency $\omega$. Because $K_{EFF}$ exceeds $K_{SF}$ at any frequency, the clamp circuit effectively stiffened the fiber in the frequency range over which the feedback circuit operated. Although the impedance of the fiber depended on frequency, it remained approximately constant at frequencies from a few hertz to $-50$ Hz with the parameter settings used in these experiments. Because most of the spectral power of the oscillation of a bundle lay within this frequency band, the fiber effectively provided a linear stiffness.

Data collection and analysis. Stimulation and recording were performed under the control of a computer (P6400 GX1; Dell Computer Corp., Round Rock, TX) running LabVIEW software, version 5.0 (National Instruments, Austin, TX). Stimulus commands and experimental control signals were provided by a dedicated interface (AT-AO-10; National Instruments). Before sampling, responses were low-pass-filtered with an eight-pole Bessel anti-aliasing filter adjusted to a half-power frequency of $1$ kHz. A multipurpose interface card (PCI-MIO-16E-1; National Instruments) conducted signal acquisition and analog-to-digital conversion with a precision of $12$ bits and a sampling rate of $2.5$ kHz.

To characterize the spontaneous oscillation of a hair bundle, we computed its power spectrum and fitted it with a Lorentzian function (Martin et al., 2001). The peak frequency of the best fit defined the frequency of the oscillation, and the half-width of the Lorentzian at half its maximal value described the extent of frequency fluctuation.

Data were analyzed with Mathematica, version 4.0 (Wolfram Research, Inc., Champaign, IL) and Matlab, version 6.0 (The MathWorks, Natick, MA).

Results

Spontaneous hair bundle oscillation

When mounted in a two-compartment experimental chamber with artificial endolymp or NMDG endolymp bathing the apical surface and standard saline solution contacting the basolateral aspect, the saccular macula from a bullfrog remained healthy for several hours. In most preparations, hair bundles were observed by eye to undergo spontaneous oscillations. In occasional preparations, all of the dozen or so hair bundles within a microscopic field of view could be seen to oscillate. The movements could also be documented by video microscopy. Slow-motion replay revealed fast bundle strokes that looked like instant jumps for a video acquisition rate of $30$ frames per second; after each stroke, the bundle remained nearly still before it leapt back in the opposite direction. Subtraction of successive video frames clearly revealed the two components of the motion of a hair bundle in each direction (Fig. 1).

We monitored the movement of an individual hair bundle by attaching the distal end of a fine glass fiber to the top of its kinocilium and projecting an enlarged image of the tip of the fiber onto a dual photodiode. Although loading a hair bundle with a fiber affects the amplitude and frequency of the oscillation (see below), the use of a very flexible fiber minimized this interference and allowed accurate measurement of the dynamical behavior of a bundle.

Different bundles were observed to oscillate spontaneously at frequencies of $5$–$50$ Hz with a peak-to-peak magnitude of motion as great as $80$ nm but most commonly $-25$ nm (Fig. 2). There was no rigorous correlation between the frequency and magnitude of spontaneous movements by different hair bundles. Two hair bundles that oscillated at frequencies almost an order of magnitude apart displayed movements of similar magnitudes (Fig. 2A,G). The slow oscillations were often the largest, however,
especially for a given hair bundle. We sometimes observed an oscillation that reversibly changed its behavior within short periods. A hair bundle that initially oscillated at \( \sim 44 \) Hz, for instance, displayed movements at \( \sim 28 \) Hz 1 min later before almost doubling its frequency to \( \sim 53 \) Hz after another 1 min had elapsed (data not shown). Correspondingly, the amplitude of oscillation increased from 18 to 30 nm before returning to 16 nm. Some bundles produced movements of almost metronomic regularity (Fig. 2A, B); others moved sporadically and occasionally halted for variable intervals (Fig. 2C).

Particularly for hair bundles that moved regularly and at relatively low frequencies, it was apparent that each cycle of spontaneous oscillation comprised movements on two time scales (Martin et al., 2000), a behavior typical of a relaxation oscillation (Strogatz, 1994). In each half-cycle, a rapid stroke was followed by a slow excursion in the same direction (Fig. 2E). The fast component generally consisted of a displacement lasting no more than 5 msec. The shape of the slower component varied from cell to cell. In some instances, the movement was nearly exponential (Fig. 2E). On other occasions, the bundle was almost stationary during this component (Fig. 2F). Finally, the trajectory was often more complex and sometimes even nonmonotonic (Fig. 2D, G). Moreover, the waveforms of the positively and the negatively directed slow components were often dissimilar (Fig. 2C, D).

Relation of channel open probability to spontaneous oscillation

By making tight-seal voltage-clamp recordings, we were able to measure changes in transduction current associated with the movement of hair bundles. In 10 spontaneously oscillatory hair cells, but not static ones, the current displayed well defined oscillations \( \sim 100 \) pA in peak-to-peak magnitude. Like spontaneous hair bundle displacements, slow current oscillations alternated between rapid transitions and relatively static intervals (data not shown).

We were able to make simultaneous tight-seal electrical recordings and mechanical measurements from one hair cell and therefore to examine the relation of transduction channel gating to bundle movement. The transduction current was highly correlated with the phase of spontaneous bundle movement. Positive bundle motion corresponded to an increase in the inward transduction current, whereas negatively directed motion coincided with decreased current (Fig. 3A). Within the temporal resolution of the mechanical and electrical recording techniques, the rapid components of bundle movement and the quick steps in transduction current occurred simultaneously. Because the current oscillations were eliminated by saturating mechanical stimuli, they represented the activity of mechanoelectrical transduction channels.

By applying large mechanical stimuli of both polarities to the hair bundle, we were able to determine the maximal transduction current with all channels open and the zero current with all channels shut (Fig. 3B). Comparison of these values with the extreme values of the transduction current measured during spontaneous oscillation revealed that the open probability varied between 0.13 and 0.70 in this spontaneously active cell.

On excitation with current pulses, a hair cell from the bullfrog’s sacculus displays damped oscillations of its membrane potential, a phenomenon termed electrical resonance. Hair cells are also capable of spontaneous electrical oscillation in the absence of stimulation. Because changing the membrane potential of a hair cell evokes bundle movements (Assad and Corey, 1992; Denk and Webb, 1992; Ricci et al., 2000, 2002; Bozovic and Hudspeth, 2003), we were concerned that hair bundle oscillation might have been the result, rather than the source, of an electrical oscillation in the soma of the hair cell. Our observation that hair bundle oscillations remain under voltage-clamp circumstances demonstrates that electrical resonance is not involved in their production.
Effect of gentamicin on spontaneous oscillation

An oscillatory hair bundle evinces a peculiar mechanical feature: its displacement–force relation, obtained by measuring the external force required to move the bundle through various distances, displays a region of negative stiffness (Martin et al., 2000). According to the gating–spring model of mechanoelectrical transduction (Corey and Hudspeth, 1983) (for review, see Markin and Hudspeth, 1995; Hudspeth et al., 2000), direct mechanical gating of transduction channels is expected to reduce the stiffness of a bundle over a limited range of positions (Howard and Hudspeth, 1988). For suitable values of the parameters of the model, this gating compliance can be great enough to dominate the other elastic components of the bundle and to render the stiffness of the bundle negative (Denk et al., 1992) (for review, see Markin and Hudspeth, 1995). Aminoglycoside antibiotics are known to block transduction channels (Kroese et al., 1989). By preventing channel gating, these drugs abolish gating compliance (Howard and Hudspeth, 1988) and should thus eliminate the negative stiffness of spontaneously oscillating bundles.

A spontaneously active hair bundle characteristically displayed a region of negative stiffness encompassing a displacement range of ~20 nm (Fig. 4A). When the solution bathing the apical hair cell surface was replaced by artificial endolymph containing 60 μg/mL gentamicin, the bundle instead behaved as a Hookean spring throughout the range of deflections explored. The region of negative stiffness of the bundle was restored by exchanging the bath with gentamicin-free endolymph.

Active mechanical biasing of a hair bundle into its unstable region of negative stiffness can explain spontaneous oscillations (Martin et al., 2000). By eliminating negative stiffness, aminoglycosides would be expected to remove one of the conditions necessary for spontaneous oscillation. On iontophoretic application of gentamicin near the top of an oscillatory hair bundle, we found that the movements reversibly disappeared (Fig. 4B). Gentamicin arrested the hair bundle in a positive position, where most transduction channels are likely to be open (Fig. 3). This observation thus confirms the previous inference that gentamicin blocks transduction channels in an open state (Denk et al., 1992; Jaramillo and Hudspeth, 1993). By blocking Ca$^{2+}$ entry through open transduction channels, gentamicin should also interfere indirectly with the myosin-based molecular motors that effect adaptation to sustained stimuli (Eatoeh et al., 1987; Hacohen et al., 1989). After the initial blockage, a hair bundle often moved slowly in the negative direction, a phenomenon attributable to mechanical adaptation when Ca$^{2+}$ entry was interrupted (Denk et al., 1992; Jaramillo and Hudspeth, 1993).

Effect of pharmacological agents on spontaneous oscillation

If spontaneous hair bundle oscillation involves the shape of the displacement–force relation of the bundle and the activity of adaptation motors, drugs that affect either would be expected to influence oscillation. Substances that interfere with the cAMP second messenger pathway evoke a shift of the transduction current–displacement curve (Ricci and Fettiplace, 1997; Géloëc and Corey, 2001) and are therefore suitable reagents with which to perturb oscillation. A wealth of information suggests that the molecular motors responsible for adaptation of the mechanoelectrical–transduction process are based on myosin molecules (for review, see Hudspeth and Gillespie, 1994; Gillespie and Corey, 1997; Eatoeh, 2000; Holt and Corey, 2000). Substances that interfere with force production by myosin would thus be expected to affect oscillation. An example is butanedione monoxime, which places myosin II molecules in a weakly bound state (Herrmann et al., 1992; Seow et al., 1997; Tesi et al., 2002). Although the effect of this substance on other myosin isoforms remains uncertain (Cramer and Mitchison, 1995; Ostap, 2002; Titus, 2003), butanedione monoxime lowers the open probability of transduction channels in hair cells (Wu et al., 1999) and may therefore affect adaptation motors.
The greatest increases in Ca\(^{2+}\) concentration attained by iontophoresis were 250 μM, or when it fell below 100 μM, the oscillations disappeared. This effect was reversible, however, because reimpoding a Ca\(^{2+}\) concentration near 250 μM restored well defined bundle oscillations.

We performed additional experiments in which we used iontophoresis to rapidly raise or lower the Ca\(^{2+}\) concentration near the stereociliary tips while keeping the glass fiber attached to the kinociliary bulb. Transiently elevating the concentration with a Ca\(^{2+}\)-containing electrode had three consistent and reversible effects: a hair bundle displayed a net movement in the negative direction; the amplitude of oscillation declined; and the frequency of oscillation increased (Fig. 6A). For small to moderate levels of iontophoresis, it was noteworthy that the increase in oscillation frequency involved principally a shortening of the slow component of movement in the positive direction. For a given bundle, the fastest oscillation that we could elicit by Ca\(^{2+}\) iontophoresis occurred at approximately twice the frequency of the control movement. The oscillation amplitude was not as strongly affected, decreasing by ~20%.

The greatest increases in Ca\(^{2+}\) concentration attained by iontophoresis suppressed rhythmic hair bundle activity (Fig. 6B). However, erratic, rapid movements lasting no more than 1–2 msec persisted. Because these spikes were distinct from the back-
ground noise apparent under control conditions during the slow components of oscillation, they probably represented residual active bundle motion. At the conclusion of the iontophoretic pulse, the oscillation resumed progressively, further demonstrating the relation among movement amplitude, frequency, and the duration of the positive phase of bundle movement. The use of iontophoretic pulses of varying intensity or the application of a ramp of iontophoretic current disclosed that a progressive increase in Ca$^{2+}$ concentration evokes graded effects (Fig. 6C).

We were also able to lower transiently the local Ca$^{2+}$ concentration around a hair bundle by iontophoresis of a chelator. Because carboxylate Ca$^{2+}$ chelators damage the transduction process by breaking tip links (Assad et al., 1991; Crawford et al., 1991; Marquis and Hudspeth, 1997), we elected to use ATP to sequester Ca$^{2+}$ (for review, see Fabiato and Fabiato, 1979). The effects of applying this nucleotide were opposite those of Ca$^{2+}$ iontophoresis. For low to modest levels of iontophoresis, the bundle displayed an offset in the positive direction and a graded slowing of spontaneous oscillations dominated by protraction of their slow component of positive motion (Fig. 6D, E). The ATP ejected by stronger iontophoretic currents entirely suppressed oscillations, producing a significant bundle excursion in the positive direction (Fig. 6F).

Effect of bundle position on spontaneous oscillation

By applying step displacements at the base of a flexible stimulus fiber, we analyzed the effect on a spontaneously oscillating hair bundle of deflected by distances up to ± 200 nm. Large offsets completely but reversibly suppressed the oscillation (data not shown). For bundle displacements smaller than ± 150 nm in either direction, however, a bundle remained quiescent only transiently (Fig. 7). During this period, the hair bundle relaxed slowly in the direction of the stimulus with a time course characteristic of mechanical adaptation (Eaton et al., 1987; Hacohen et al., 1989). After the bundle position had attained a plateau and adaptation had presumably concluded, the oscillation eventually resumed.

The recovery of oscillation during a protracted displacement could be abrupt for small bundle offsets but was graded for larger ones. In the latter case, oscillation grew progressively over the course of a few cycles from zero amplitude to a steady-state level and correspondingly decreased its frequency. The recovery was not complete, however, in that the oscillation was consistently faster than at rest when the bundle was offset in the positive direction and slower when it was displaced in the negative direction. In contradistinction to the effect of changes in Ca$^{2+}$ concentration near the stereociliary tips, bundle offset affected primarily the slow component of negative movement. The symmetry of oscillation was modified in such a way that a bundle displayed spiky movements in one direction when it was offset in the other.

Effect of mechanical load on spontaneous oscillation

When attached to the flexible glass fibers used in this study, most hair bundles oscillated at frequencies near 10 Hz. These frequencies lie near the bottom of the range of 5–150 Hz that is characteristic of saccular nerve fibers (Koyama et al., 1982; Yu et al., 1991) and presumably of the corresponding hair cells. Although several aspects of in vitro recording might have perturbed the oscillation frequency, one condition whose effect could readily be tested was the elastic load against which the hair bundle operated.

While recording spontaneous bundle oscillations, we used varying degrees of negative feedback, or partial displacement clamping, to increase the effective stiffness of the stimulus fiber attached to a bundle. When the stiffness of the fiber rose, the magnitude of the oscillation of a bundle characteristically declined as the frequency of spontaneous oscillation increased (Fig. 8A). A sufficiently great increase in the effective stiffness of the stimulus fiber suppressed well defined bundle oscillations altogether (Fig. 8B).

The effect of mechanical load on the frequency and amplitude of spontaneous hair bundle oscillation bears on the status of unstimulated bundles in vivo. Like those in most acousticolateralis organs, a hair bundle of the bullfrog’s saccus is normally at-
attached to an accessory structure. In the intact ear, the bulbous tip of the single kinocilium in the bundle is linked by numerous filaments to the compact layer of the otolithic membrane (Hilman and Lewis, 1971; Jacobs and Hudspeth, 1990; Kachar et al., 1990). The polycrystalline otoconia that surmount this structure constitute an inertial mass whose movement relative to the skull signals acceleration. Although the mechanical properties of the otolithic membrane are complex (Benser et al., 1993), the structure exhibits a steady-state stiffness of 1400 ± 800 μN·m⁻¹ for each of the ~2500 attached hair bundles. The present results suggest that the stiffness of the otolithic membrane is comparable with the minimal load required to suppress spontaneous oscillation.

Role of the kinocilium in spontaneous oscillation
In addition to the clustered stereocilia that mediate mechanoelectrical transduction (Hudspeth and Jacobs, 1979), every hair bundle, at least during its development, includes a single kinocilium. Because it contains an axoneme, or 9 + 2 array of microtubules adorned with dynein motor molecules, a kinocilium is capable of performing mechanical work. A kinocilium can oscillate spontaneously (Bowen, 1931) and can move in response to electrical stimulation (Rüschi and Thurm, 1990). Because this organelle has been suggested to contain the motor molecules responsible for hair bundle oscillation (Camata et al., 1999, 2000), we wished to determine its role in the process.

A kinocilium may be detached from the stereociliary cluster by microdissection with the tip of a microelectrode (Hudspeth and Jacobs, 1979). We selected hair bundles that displayed robust spontaneous oscillations in artificial endolymph solution. After the kinocilium had been detached from each of five such bundles, all continued their active movements (Fig. 9). Even flattening the kinocilium against the apical surface of the hair cell and holding it pointed away from the stereociliary cluster with the dissecting electrode did not arrest spontaneous movements. In most instances, the magnitude of the oscillation increased slightly after dissection. This response might indicate that a kinocilium imposes a load on the stereociliary cluster (Crawford and Fettiplace, 1985). The change after dissection might alternatively stem from repositioning of the stimulus fiber at the top of a bundle, slightly farther from the apical surface of the cell than the control point of attachment at the kinociliary bulb.

Model for spontaneous hair bundle oscillation
To ascertain whether our understanding of the principal features of spontaneous hair bundle oscillation accords with the present experimental findings, we developed a model for oscillations and tested its performance in simulations of several experimental conditions. More specifically, we assembled equations to represent hair bundle mechanics, mechanoelectrical transduction and the flow of ionic current, adaptation of the transduction process, and Ca²⁺-dependent channel reclosure. We did not include the effects of noise in the model. These equations, their origins and justifications, and other features of the model are described in the Appendix.

The model yields simulated oscillations resembling those observed experimentally. In particular, adjustment of parameter values within a range that accords with other measurements readily produces oscillations of frequencies extending throughout and beyond the observed range of 5–50 Hz and of peak-to-peak magnitudes up to 70 nm. The oscillation waveforms resemble those of actual bundle movements (Fig. 10 A, B). Each phase of the slower oscillations is bipartite, with a rapid initial component followed by a slow relaxation. As for actual oscillations, the slow components may be approximately exponential, essentially flat, or even nonmonotonic.

Changing the extracellular Ca²⁺ concentration affects simulated oscillations as it does actual bundle movements. In particular, an abrupt increase in Ca²⁺ concentration, similar to that during iontophoretic application of the ion, accelerates oscillations by shortening the slow component of positive motion and reduces their magnitude (Fig. 10 C). A comparable concentration decrease, which mimics the effect of iontophoretic ejection of a Ca²⁺ chelator, slows oscillations by prolonging the slow component of positive movement and augments their size (Fig. 10 D).

The formulation of the model for the mechanism of Ca²⁺-dependent channel reclosure was meant to encompass the experimental observation that the amplitude of oscillation changes in response to alterations of the extracellular Ca²⁺ concentration. If each cycle of oscillation represents a trajectory around the displacement–response relation (Martin et al., 2000), its amplitude can be changed only by adjusting the shape of the relation. In the present model, Ca²⁺ entry into the stereociliary cytoplasm relaxes a component of the gating spring, thus reducing the magnitude of negative stiffness and shortening the oscillatory trajectory. The response of the model to simulated Ca²⁺ exposure captures this aspect of the experimental result.

The model also recapitulates the effects of increasing the mechanical load on a hair bundle. As the stiffness of the fictive stimulus fiber increases, oscillation becomes faster and smaller (Fig. 10 E) until it is wholly suppressed.

Modeling readily simulates the effects of pharmacological reagents on spontaneous hair bundle oscillation. Reducing the rate of adaptation motor climbing lowers the frequency of oscillation.
admits Ca\textsuperscript{2+} entry diminishes and the bundle becomes stiffer. As a result, the displacement–force and displacement–open probability relations of the bundle continuously adjust their shapes during the oscillation, causing the trajectories of the bundle in the two directions to display hysteresis. This effect potentially explains the measured asymmetry of the open probability oscillation (Fig. 3).

A few features of the experimental results are not represented in the simulations. In response to an increased or decreased Ca\textsuperscript{2+} concentration, for example, hair bundles display gradual changes on a time scale of hundreds of milliseconds (Fig. 6). These responses may reflect stereociliary Ca\textsuperscript{2+} homeostasis (Lumpkin and Hudspeth, 1998; Ricci et al., 1998; Yamoh et al., 1998), which has been omitted from the model. Perhaps for the same reason, the model cannot reproduce the slow, progressive recovery of oscillations after large bundle offsets (Fig. 7).

**Discussion**

In a simple model, only two ingredients are necessary to endow a hair bundle with the ability to oscillate spontaneously: a region of negative stiffness in the displacement–force relation of the bundle and a biasing element, such as the adaptation motor, that forces the bundle into this unstable region (Martin et al., 2000). The present results support this model by confirming several predictions based on it. In addition, they reveal that the negative stiffness of the hair bundle and the adaptation motor are both affected by external perturbations, suggesting potential regulatory mechanisms by which active hair bundle motility might optimize the response of a hair cell to mechanical stimulation.

**Relation of oscillation to transduction channel gating**

The negative stiffness of a hair bundle originates from gating compliance, a reduction in stiffness associated with the mechanical gating of transduction channels (Howard and Hudspeth, 1988) (for review, see Hudspeth et al., 2000). It therefore stands to reason that bundle oscillation is abolished by blockage of transduction channels with gentamicin, a procedure that arrests channel gating and thereby eliminates negative stiffness (Fig. 4).

Our electrical recordings also concur with theory by associating the positive phase of bundle movement with channel opening and the negative with closure. The results are consistent with the hypothesis that channel gating provides one of the forces that generate hair bundle motion.

The magnitude of oscillation depends on the trajectory that an active hair bundle executes with respect to its displacement–force relation (Fig. 11). In principle, the size of an oscillation depends on the magnitude of the gating compliance of a bundle relative to the combined stiffness of the other elastic components of the bundle and the load. Increasing the elastic load applied to the bundle would be anticipated to diminish the oscillations until it suppresses them altogether. Both the experimental result (Fig. 8) and the simulation (Fig. 10E) accord with this expectation. Al-
to oscillate at 11 nm (top record). Another hair bundle, which originally oscillated at 9 nm with a magnitude of 12 nm (top record), survived microsurgery with oscillations at 10 Hz and 16 nm in magnitude (bottom record).

alternatively, reduced gating compliance would flatten the displacement–force relation and yield smaller oscillations.

Participation of myosin in oscillation

Adaptation by the mechanoelectrical transduction process of the bullfrog’s hair cells is mediated by myosin molecules, in particular myosin Ic (for review, see Hudspeth and Gillespie, 1994; Gillespie and Corey, 1997; Eaton, 2000). The success of the model at simulating most of the present results reinforces the previous inference (Martin et al., 2000) that the combination of adaptation motors and negative bundle stiffness underpins spontaneous hair bundle oscillation.

Phosphorylation of proteins associated with transduction channels, including the channels themselves, could explain the effects of drugs that interact with the cAMP signaling pathway. In particular, cAMP analogs and other substances that affect the activity of protein kinase A, and the phosphorylation of its targets might influence myosin-based adaptation motors, whose activity contributes to setting the operating point of transduction (Hacohen et al., 1989). In many cells, $\text{Ca}^{2+}$ interacts with calmodulin to activate adenyl cyclase, producing cAMP that stimulates protein kinase A. This enzyme then phosphorylates the target proteins that constitute the effectors of the pathway. In the present instance, it is attractive to hypothesize that the operation of adaptation motors is impeded by the phosphorylation of myosin Ic at a consensus target site, such as serine 701 of the bullfrog's

myosin Ic (Metcalf et al., 1994; Solc et al., 1994; G. Géléc, P. Gillespie, and D. Corey, personal communication).

Butanedione monoxime blocks spontaneous hair bundle oscillation. Because this substance interferes with the ATPase cycle of myosin II (Herrmann et al., 1992; Seow et al., 1997; Tesi et al., 2002), this effect may reflect the arrest of myosin-based adaptation motors. This inference must be qualified, however, because the substance affects other physiological processes as well. Bu-
The displacement–force relation at the top left (green curve) shows the instantaneous stimulus fiber force ($F_{sf}$) necessary to hold the hair bundle at a given position ($x$), as set by a displacement-clamp apparatus. This relation is specified by the steady-state solution of Equation 5 with $x_0 = 0$. The region of negative stiffness corresponds to most of the range of bundle positions in which transduction channels are moving between their closed and open states, as revealed by the dependence of $p_o$ on bundle displacement represented by the continuous line at the bottom left. The adaptation motor strives to position the hair bundle near the middle of the displacement–force relation, in this instance at $p_o = 0.35$. Because it is unstable in the region of negative slope stiffness, however, the hair bundle is destined to oscillate. The red arrows delineate the trajectory of bundle movements corresponding to the oscillation at the top right. Any perturbation that nudges the bundle into to the right part of the negative-stiffness region oblige the bundle to lurch in the positive direction (step 1). As shown in the plot of open probability against time at the bottom right, this movement raises the open probability of the transduction channel to $0.8$. When mechanical instability prompts another fast component of movement in the negative direction (step 3), the open probability of the channel falls to $0.1$ while completing a cycle of oscillation (step 4). Note that the plots of force and open probability against displacement represent steady-state relations with a fixed value for the gating spring stiffness, $1500 \, \mu N \cdot m^{-1}$, a characteristic of an open probability of $0.35$. During the positive phase of each cycle of oscillation, however, the effect of $Ca^{2+}$ entry on the reclosure element decreases the gating spring stiffness from a maximal value of $1143 \, \mu N \cdot m^{-1}$ to a minimum of $808 \, \mu N \cdot m^{-1}$. As a consequence and in agreement with the experimental results (Fig. 3), the simulated excursion of open probability in the time domain is asymmetrical. The displacement–force relation and oscillation correspond to the values of Table 1 but with $K_{g} = 0 \, \mu N \cdot m^{-1}$. The range of open probabilities from $0$ to $1$ is calibrated by the extremes of the steady-state relation of open probability to displacement. When the bundle is attached to a stimulus fiber of stiffness $K_{g} = 150 \, \mu N \cdot m^{-1}$, its oscillation follows a trajectory whose fast components parallel the load line of slope $-K_{g}$ (blue line). The resultant bundle movement, which is smaller than that in A and occurs at a greater frequency, corresponds to the values in Table 1. The displacement–open probability relation in this instance is identical to that in A. C. By altering the shape of the displacement–force relation, $Ca^{2+}$ also affects the magnitude, frequency, and waveform of spontaneous oscillation. Bundle movements become smaller and faster when the single-channel gating force, $z = \gamma K_{g} d$, is decreased by a diminution in either the maximal stiffness of the reclosure element, here $K_{g,\text{max}} = 860 \, \mu N \cdot m^{-1}$ (oscillation at right and dotted green curve at left), or the gating distance, here $d = 5.2 \, nm$ (dashed green curve at left). Note that in the first case, both the static stiffness and maximum negative stiffness of the bundle are reduced, whereas in the second case, only the negative stiffness is affected (compare A, C). The remaining parameter values correspond to those in Table 1, again with $K_{g} = 0 \, \mu N \cdot m^{-1}$. The displacement–open probability relations for these circumstances are shown at the bottom left in A; the curve for diminished stiffness is dotted, and that for reduced gating distance is dashed. The identical vertical and horizontal distance calibrations apply to the abscissas of all graphs as well as to the simulated oscillations.

Tanedione monoxime broadens the displacement–transduction current relation of a bundle (Wu et al., 1999), suggesting that gating compliance is diminished, so the blockage of oscillation might reflect a decrease in the negative stiffness of the bundle. The compound can also block ion pumps (Tucker and Fettiplace, 1996) that might influence stereociliary $Ca^{2+}$ homeostasis.

**Effects of $Ca^{2+}$ on oscillation**

Altering the $Ca^{2+}$ current that enters the stereociliary cytoplasm through transduction channels has an immediate effect on oscillation: $Ca^{2+}$ affects the duration of the slow component of positive movement (Fig. 6). Because this component is thought to be mediated by slippage of myosin-based adaptation motors down the stereocilia, our observations buttress previous evidence that an increased $Ca^{2+}$ concentration facilitates detachment of the myosin molecules from actin (Hacohen et al., 1989; Assad and Corey, 1992). The activity of the motor is relatively unaffected by extracellular $Ca^{2+}$ during the negative slow component of oscillation, when most of the channels are closed.

The decrease of the oscillation magnitude (Fig. 6A,B) in response to $Ca^{2+}$ iontophoresis may readily be modeled by rendering the stiffness of some component of the gating spring sensitive to $Ca^{2+}$ (Fig. 10C). Removal of extracellular $Ca^{2+}$ with a chelator has the opposite effect (Figs. 6D, E, 10D).

The shift of the mean position of a bundle when the extracellular $Ca^{2+}$ concentration is elevated probably results from an adaptive response to a change in the average $Ca^{2+}$ concentration at the adaptation motor. Because this treatment reduces the open time of the channels, $Ca^{2+}$  iontophoresis may lower the average intracellular $Ca^{2+}$ concentration. The adaptation motor would then ascend the stereocilia, increasing the gating spring tension and thus evoking a negative shift. Because our model does not include a description of $Ca^{2+}$ homeostasis, however, our simulation does not reproduce this effect.

When the $Ca^{2+}$ concentration is either too high or too low, a hair bundle becomes quiescent. At these concentrations, the displacement–force relation of the bundle might not display an unstable region of negative stiffness (Howard and Hudspeth, 1988). Alternatively, the channel open probability at which the adaptation motors reach their steady state might lie outside the region of instability. If the open probability lies on the brink of the negative-stiffness region, however, noise would occasionally push the bundle into this region, triggering arrhythmic twitches (Fig. 6B). Because the magnitude of these twitches remains comparable with that of control oscillations, the negative-stiffness region probably persists at higher $Ca^{2+}$ concentrations.

**Adjustment to an Hopf bifurcation**

Active hair bundle motility appears to operate near a Hopf bifurcation that separates the quiescent and spontaneously oscillatory regimens of a bundle (Martin and Hudspeth, 2001). Because a dynamical system provides optimal amplification and frequency discrimination when operating near the bifurcation (Choe et al., 1998; Eguiuz et al., 2000), it might be expected that a negative-feedback mechanism holds it there (Camata et al., 2000). The response of an oscillatory bundle to protracted displacements indeed reveals the operation of such feedback. After having been transiently suppressed by these stimuli, spontaneous oscillation progressively resumes (Fig. 7). During recovery, the oscillation magnitude grows from zero, primarily by increasing the size of the rapid components of bundle movement. Because these components correspond to jumps across the negative-stiffness region of the displacement–force relation of the bundle (Martin et al., 2000), their magnitude depends on the breadth of this region of instability. To accord with our observations, this region must expand as the oscillation recovers. Negative stiffness arises when gating compliance dominates other elastic components in the hair bundle, so our results suggest that the gating force can be regulated.

The myosin molecules underlying adaptation could themselves be regulators of the bifurcation. A few dozen of these, apparently myosin Ic molecules (Gillespie et al., 1993; Holt et al., 2002), are thought to link each transduction channel to the actin
Gating could also be controlled by allowing Ca\textsuperscript{2+} to affect the state of transduction channels directly, channel reclosure of transduction channels might then power spontaneous Ca\textsuperscript{2+} element and on the fraction of motors attached to actin filaments. Its effective stiffness would depend both on the elasticity of each mechanical elastic structure that could be part of the gating spring.

The core of the stereocilia. This ensemble of motors provides a dynamical elastic structure that could be part of the gating spring. Its effective stiffness would depend both on the elasticity of each element and on the fraction of motors attached to actin filaments at any time. Either of these parameters is potentially sensitive to Ca\textsuperscript{2+}; the duty cycle of adaptation motors would be regulated through the cAMP second-messenger pathway (Ricci and Fettiplace, 1997), or Ca\textsuperscript{2+} binding to calmodulin might affect the stiffness of the myosin neck (Howard and Spudich, 1996; Gillespie and Corey, 1997).

Matching the negative stiffness of a hair bundle to the positive stiffness of the load would allow the bundle to operate at a Hopf bifurcation. Because the myosin-based adaptation motors would approach a steady state under these circumstances, Ca\textsuperscript{2+}-mediated reclosure of transduction channels might then power spontaneous oscillations (Choe et al., 1998). Although Ca\textsuperscript{2+} was originally posited to affect the state of transduction channels directly, channel gating could also be controlled by allowing Ca\textsuperscript{2+} to regulate the stiffness of gating springs. This arrangement would endow the gating spring with an intracellular component sensitive to Ca\textsuperscript{2+}.

In the frog’s saccule, where each hair bundle is attached to an otolithic membrane, precise matching of the negative stiffness of the bundle to the positive stiffness of the membrane is improbable. The hair cell may thus require the capacity to adjust the stiffness of the bundle over a limited range. The responses shown here demonstrate that hair bundles in fact possess mechanisms for responding to various perturbations. The hair bundles of most receptor organs are attached to an accessory structure such as a tectorial or an otolithic membrane, a sallet, or a cupula. The capacity to adjust hair bundles to operate at a Hopf bifurcation may therefore prove to be a general characteristic of hair cells that ensures optimal performance.

### Appendix

We modeled spontaneous hair bundle oscillations in the absence of noise by developing equations to represent four component processes: hair bundle mechanics, mechanoelectrical transduction and the associated ionic current, adaptation of the transduction process, and Ca\textsuperscript{2+}-dependent channel reclosure. Here we present the essential equations of the model and explain the rationale for choosing them. We additionally provide representative values for the parameters of the model (Table 1) and cite their sources. A copy of the Mathematica program for the model is available on request.

#### Hair bundle mechanics

The hair bundle is represented as an elastic structure with a specific mass, moving at a low Reynolds number through a viscous medium under the influence of force delivered by an external stimulus fiber and of forces internal to the bundle. At any time, the balance of forces acting at the tip of the kinocilium, where the fiber is attached, requires that the force exerted by the stimulus fiber, \( F_{SF} \) be:

\[
F_{SF} = K_{SF}(\Delta - X)
\]

\[
= (m_{HB} + m_{SF})\frac{d^2X}{dt^2} + (\xi_{sm} + \xi_{so}) \frac{dX}{dt} + N_{CS} y \kappa_{CS}(\gamma X - x_s + x_c - p(d)) + K_{SP}(X - X_{SP}),
\]

where the symbols are defined in Table 1.
in which $X$ represents the position of the top of the bundle as well as that of the tip of the fiber (Howard and Hudspeth, 1988; Benser et al., 1996). Stimuli are applied through a fiber of stiffness $K_{SSP}$ whose base is displaced by a distance $\Delta$ with the stimulator. $m_{SSB}$ and $m_{SSP}$ are, respectively, the masses of the bundle and of the relevant part of the attached stimulus fiber with the entrained fluid. In the overdamped regimen germane to the present low-frequency measurements, these masses are unimportant; they are included for the sake of completeness and to allow extension of the model to higher frequencies of stimulation. $\xi_{SSB}$ and $\xi_{SSP}$ are the corresponding drag coefficients. Because the base of the stimulus fiber was stationary during most measurements of spontaneous hair bundle motion, we have neglected an additional drag coefficient attributable to fluid flow caused by the base movements of the fiber (Martin et al., 2001). The $N_{GS}$ transduction elements, each comprising a gating spring of stiffness $K_{GS}$ attached to the gate of a single transduction channel, are assumed to lie in parallel with one another and to experience identical mechanical inputs (Howard et al., 1988; Jacobs and Hudspeth, 1990; Iwasa and Ehrenstein, 2002). The exact distribution of channels between stereocilia and their positions with respect to the ends of tip links are immaterial to the model. The geometrical gain $\gamma$ relates the shearing motion between contiguous stereocilia, and hence gating spring extension, to movement at the top of the bundle. In the initial state of the hair bundle, the gating spring experiences an extension of $x_c$ when the channel is closed (Jaramillo and Hudspeth, 1993). Opening of the channel shortens the gating spring by a distance $d$; positive adaptation shortens it by an amount $x_c$. At any instant, the open probability of the channel is $p_O$; the total extension of the gating spring is $\gamma X - x_c - p_O d$. The bending of each stereocilium at its base is opposed by the elasticity of the actin fascicle that extends as a rootlet into cuticular plate (Crawford and Fettiplace, 1985; Howard and Ashmore, 1986). The stiffness of the ensemble of these stereociliary pivots is $K_{SP}$ (Howard and Hudspeth, 1988; Marquis and Hudspeth, 1997). When the tip links are severed, the hair bundle relaxes to the equilibrium position of those pivots, $X_{SP}$ (Howard et al., 1988; Assad et al., 1991).

**Mechanoelectrical transduction and Ca$^{2+}$ entry**

The gating of the transduction channels in a hair bundle is described by the gating spring model (Corey and Hudspeth, 1983) (for review, see Howard et al., 1988; Hudspeth, 1992; Markin and Hudspeth, 1995; Hudspeth et al., 2000). The open probability of each transduction channel is:

$$p_O = \frac{1}{1 + e^{[\Delta E^G - \kappa_{ES}(\gamma X - x_c - p_O d)/kT]}}. \tag{6}$$

The intrinsic internal energy change associated with channel gating, $\Delta E^G$, reflects the increase in energy content of a channel when it moves from the closed to the open state in the absence of a gating spring. $k$ is the Boltzmann constant, and $T$ is the temperature. Because of the rapidity of transduction on the time scale of the oscillations studied here (Corey and Hudspeth, 1983), a description of the kinetics of gating is unnecessary, and this equilibrium formulation of the open probability suffices.

The very low cytoplasmic concentration of Ca$^{2+}$ virtually precludes outward current carried by that ion, so it is unrealistic to describe the Ca$^{2+}$ current through an open transduction channel, $I_{Ca}$, in terms of a conductance and driving force. We instead use the Goldman–Hodgkin–Katz current equation (Hille, 1992):

$$I_{Ca} = p_O p_{Ca} \frac{C_{Ca} eF V_M [Ca^{2+}]}{kT [1 - e^{(\gamma X - x_c - p_O d)/kT}]} . \tag{7}$$

Here $p_{Ca}$ is the Ca$^{2+}$ permeability, $z_{Ca}$ is the valence of the ion, $e$ is the electron charge, $F$ is the Faraday constant, $[Ca^{2+}]$ is the Ca$^{2+}$ concentration in endolymph, and $V_M$ is the membrane potential.

Ca$^{2+}$ that enters the stereociliary cytoplasm through transduction channels is subject to buffering and extrusion (Lumpkin and Hudspeth, 1998; Ricci et al., 1998; Yamoah et al., 1998). The mean time to capture by buffer molecules, however, is great enough that buffering has little effect within $\sim 100$ nm of a channel (Roberts, 1993, 1994). Because an insertional plaque is only $\sim 50$ nm in diameter, we may assume that the Ca$^{2+}$-binding sites responsible for regulating motor activity are essentially exposed to Ca$^{2+}$ diffusing from a point source, the channel, into a semi-infinite volume. For a motor at a distance $r_M$ from the channel, the steady-state Ca$^{2+}$ concentration is then (Berg, 1993):

$$[Ca^{2+}] = \frac{-I_{Ca}}{2 \pi r_M F D_{Ca} z_C}, \tag{8}$$

in which $D_{Ca}$ is the diffusion coefficient of Ca$^{2+}$. This steady-state concentration is mostly achieved within a few tens of microseconds (Lumpkin and Hudspeth, 1998).

**Adaptation**

Adaptation of the mechanoelectrical transduction process (for review, see Hudspeth and Gillespie, 1994; Eatock, 2000; Holt and Corey, 2000) is assumed to result from movement of the insertional plaque at the upper end of each tip link (Howard and Hudspeth, 1987a,b). This movement is affected by two countervailing influences; the downward pull of the extended gating spring and the ascent of the myosin-based molecular motor at the insertional plaque (Assad and Corey, 1992). In addition, the insertional plaque is anchored to the stereociliary cytoskeleton by an elastic extent spring that renders adaptation incomplete (Shepherd and Corey, 1994; Yamoah and Gillespie, 1996). The rate of adaptation is:

$$\frac{dx_p}{dt} = -C + S[k_{ES}(\gamma X - x_c - p_O d) - \kappa_{ES}(x_c + x_{ES})], \tag{9}$$

in which $C$ is the rate constant for climbing adaptation (myosin-driven upward movement of the insertional plaque), and $S$ is that for slipping adaptation (downward motion attributable to tension in the gating spring). A positive value for $x_{ES}$, which reflects a decrease in gating spring tension, corresponds to movement down the stereocilium. With the hair bundle in its initial position, the insertional plaque is located a distance $x_{ES}$ below the cytoskeletal attachment of an extent spring of stiffness $\kappa_{ES}$.

The rate of adaptation depends on the stereociliary Ca$^{2+}$ concentration (Eatock et al., 1987; Crawford et al., 1989; Hacohen et al., 1989). Although the explicit dependence has not been measured, it appears that the value of the parameter $S$ increases and that of the parameter $C$ declines with an elevation of the Ca$^{2+}$ concentration (Assad and Corey, 1992; Shepherd and Corey, 1994). We suppose that Ca$^{2+}$ binds to calmodulin (Walker et al., 1993; Walker and Hudspeth, 1996) attached at the two, three, or possibly four IQ domains of each myosin Ic molecule at the ad-
aptation motor (Metcalfe et al., 1994; Solc et al., 1994). Although this ensemble of calmodulin molecules could potentially bind as many as 16 ions, we consider for the sake of simplicity only uni-molecular binding at any of a single class of sites, characterized by an ON rate constant, $k_{ON,M}$, and an OFF rate constant, $k_{OFF,M}$, and hence by a dissociation constant, $K_{D,M}$. The probability of Ca$^{2+}$ binding, $P_{BR}$, changes at the rate:

$$\frac{dp_{BR}}{dt} = k_{ON,M}[Ca^{2+}](1 - p_{BR}) - k_{OFF,M}p_{BR}.$$  \(10\)

At equilibrium, the binding probability is:

$$p_{BR} = \frac{1}{1 + \left(\frac{k_{OFF,M}}{k_{ON,M}[Ca^{2+}]}\right) \frac{K_{D,M}}{[Ca^{2+}]}}.$$  \(11\)

The activity of the adaptation motor in turn depends on the extent of Ca$^{2+}$ binding at the regulatory site. The rate constant for climbing adaptation is governed by the relation:

$$C = (1 - P_{BR})(C_{MAX} - C_{MIN}) + C_{MIN}.$$  \(12\)

Slipping adaptation is described by:

$$S = P_{BR}(S_{MAX} - S_{MIN}) + S_{MIN}.$$  \(13\)

**Ca$^{2+}$-dependent channel reclosure**

The reclosure of a mechanoelectrical transduction channel under the influence of Ca$^{2+}$ was initially hypothesized to occur when Ca$^{2+}$ binds directly to the channel itself or to a closely coupled protein and alters the energy difference between the closed and open states of the channel (Howard and Hudspeth, 1988; Jaramillo et al., 1990). Subsequent modeling has been based on this mechanism (Choe et al., 1998; Wu et al., 1999). In the present instance, we hypothesize instead that Ca$^{2+}$ in the stereociliary cytoplasm does not force a channel to shut but allows it to close. More specifically, we consider that the binding of Ca$^{2+}$ reduces the gating spring tension that promotes channel opening and thereby fosters reclosure. Three considerations motivate this formulation. First, when hair bundles are immersed in standard saline solution, the fast positive phase of their movement in response to transient mechanical stimulation (Benser et al., 1996) may reflect a rapid relaxation event in addition to a passive elastic response. Next, Ca$^{2+}$-induced relaxation of an element in the transduction machinery provides an explanation for electrically evoked hair bundle movements (Bozovic and Hudspeth, 2003). Finally, the changes in oscillation amplitude observed in the present study imply a mechanism that alters the shape of the displacement–force relation of the hair bundle. Although there may be several ways in which such a change could occur, we elected to use in the model a representation consistent with the two foregoing observations. Our formulation is not meant to preclude the possibility that the binding of Ca$^{2+}$ to the transduction channel also promotes channel reclosure more directly, but that possibility is not required in the present simulations.

We represent each gating spring as two components in series. The extracellular component is the tip link, whose stiffness, $k_{TL}$, might be quite high (Kachar et al., 2000). The intracellular reclosure element, of stiffness $k_{RE}$, might represent the elasticity of the neck domains of myosin Ic molecules at the insertion plaque (Howard and Spudich, 1996; Gillespie and Corey, 1997). Another possibility is that the stiffness of this element reflects the number of these molecules attached in parallel to the actin cytoskeleton at any time. In either event, the two elements lie in series and the overall stiffness of each gating spring is:

$$k_{GS} = \frac{k_{TL}k_{RE}}{k_{TL} + k_{RE}}.$$  \(14\)

The stiffness of the reclosure element depends on the probability of Ca$^{2+}$ binding there. The Ca$^{2+}$ concentration at a reclosure element located a distance $r_{RE}$ from a transduction channel is given by Equation 8, with the term $r_{RE}$ substituted for $r_{TL}$; the subscript RE denotes the reclosure element. The probability of Ca$^{2+}$ binding varies with time according to Equation 10, and the associated equilibrium binding probability is given by Equation 11, again with the substitution of subscripts.

For the sake of simplicity, we suppose that the stiffness of the reclosure element varies linearly between a maximal and a minimal value, respectively $k_{RE,MAX}$ and $k_{RE,MIN}$, in proportion to the probability that Ca$^{2+}$ is bound, $P_{BR,RE}$:

$$k_{RE} = (1 - P_{BR,RE})(k_{RE,MAX} - k_{RE,MIN}) + k_{RE,MIN}.$$  \(15\)

**References**


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Géléc GSG, Corey DP (2001) Modulation of mechanoelectrical transduction by protein kinase A in utricular hair cells of neonatal mice, Abstract 21903, 2001 Midwinter Meeting of the Association for Research in Otolaryngology, St. Petersburg Beach, FL.


Marquis RE, Hudspeth AJ (1997) Regulation of hair-cell transduction channels by protein kinase A in utricular hair cells of neonatal mice, Abstract 321, 2002 Midwinter Meeting of the Association for Research in Otolaryngology, St. Petersburg Beach, FL.

Manley GA, Kirk DL (2002) BAPTA reduces the frequency of spontaneous otoacoustic emissions in lizards, Abstract 321, 2002 Midwinter Meeting of the Association for Research in Otolaryngology, St. Petersburg Beach, FL.


